

Improved Inference of Causal Networks from Gene Expression Time Series

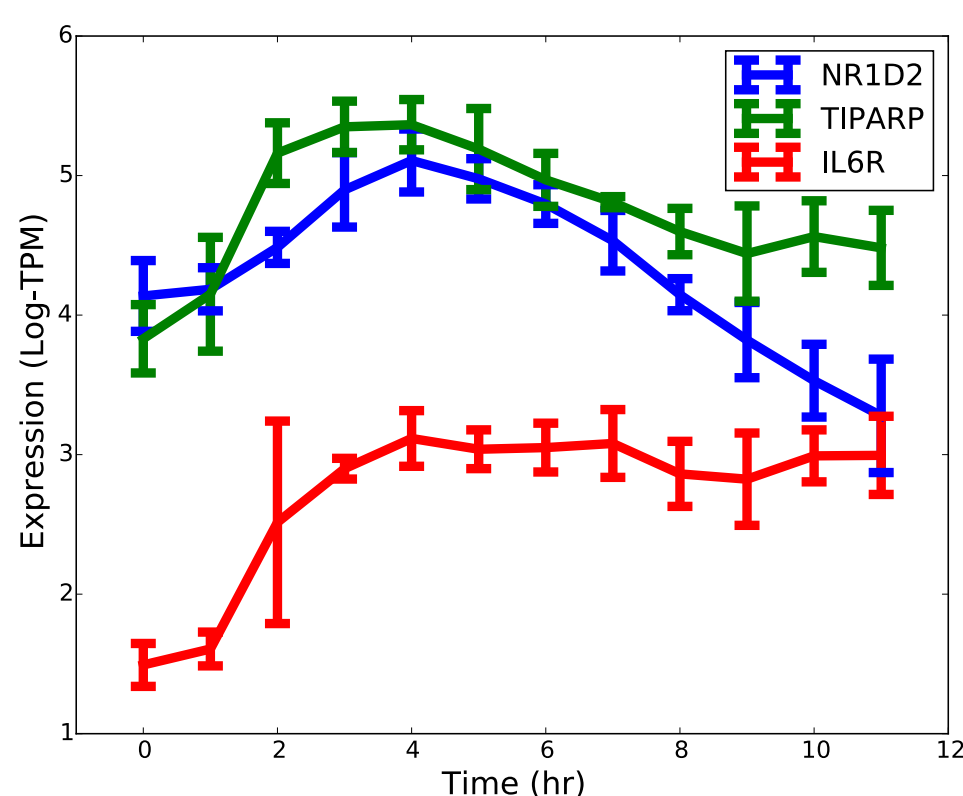
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Background

- Glucocorticoids (GCs) are immunosuppressant drugs that can lead to metabolic disorders such as diabetes and obesity
- How can we disentangle the desired immune effects from the adverse metabolic effects?
- GC binds to the glucocorticoid receptor (GR), which initiates transcription of a variety of genes, leading to a cascade of effects
- Can we infer the triggered causal network to pinpoint the immune and metabolic response?
- Use Gene expression time series from GC-stimulated lung cells
- 2768 differentially expressed genes, 12 timepoints, 4 replicates



Methodological challenges:

- **High dimensionality:** samples \ll predictors
- **Statistical significance:** F-test undefined⁵
- **Validation:** Ensure biological relevance

Goal

Build **comprehensive pipeline for causal network inference** that handles high dimensionality, maintains statistical significance, and validates on external biological data.

Prior Approaches

Previous methods either do 1) low-dimensional fit or 2) high-dimensional fit missing an effective statistical null or biological validation

	Mukhopadhyay 2007 ¹ , Tam 2012 ² , ...	Lozano 2009 ³ , Shojaie 2010 ⁴ , Yao 2015 ⁵ , ...	Our Work
High-dimensional causal fit	✗	✓	✓
Statistical significance	✓	~	✓
External validation	✗	~	✓

Vector Autoregression

Based on Granger Causality⁶ principle:
 $X \rightarrow Y$ if including past values of X helps to predict Y

- Fast, effective, flexible lags

$$Y_t = \sum_{i=1}^k \alpha_i Y_{t-i} + \sum_{i=1}^k \beta_i X_{t-i} + \epsilon_t$$

$$H_0 : \beta_i = 0 \text{ for all } i$$

High-Dimensional Fit

Fit all causes simultaneously and regularize

$$Y_t = \sum_{i=1}^k \alpha_i Y_{t-i} + \sum_{g \in G} \sum_{i=1}^k \beta_i^g X_{t-i}^g + \epsilon_t$$

$$\hat{\beta} = \arg \min_{\beta} \|Y - X\beta\|_2^2 + \lambda f(\beta)$$

$$f_{\text{LASSO}}(\beta) = |\beta|_1$$

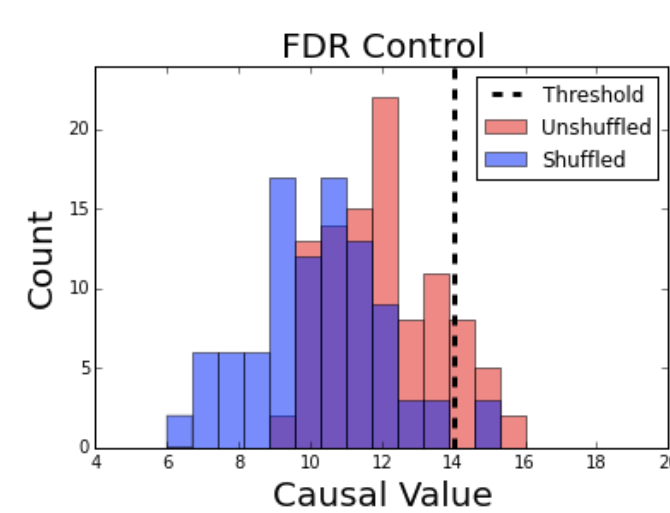
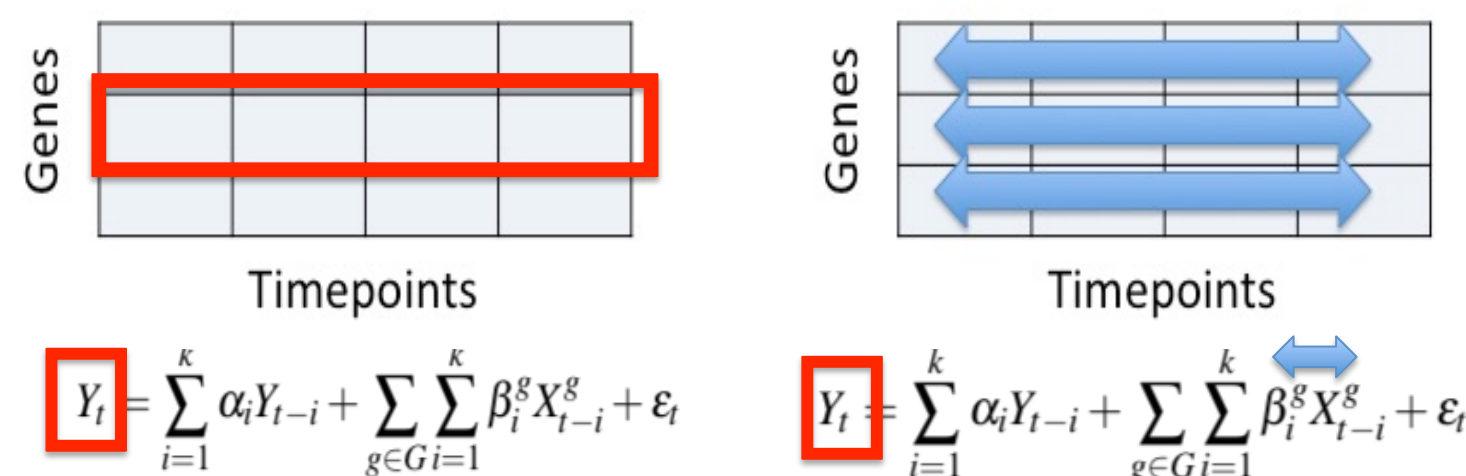
$$f_{\text{RIDGE}}(\beta) = |\beta|_2^2$$

$$f_{\text{ELASTIC}}(\beta) = \alpha |\beta|_1 + (1 - \alpha) |\beta|_2^2$$

$$H_0 : \beta_i^g = 0 \text{ for given } g \in G.$$

Statistical Significance

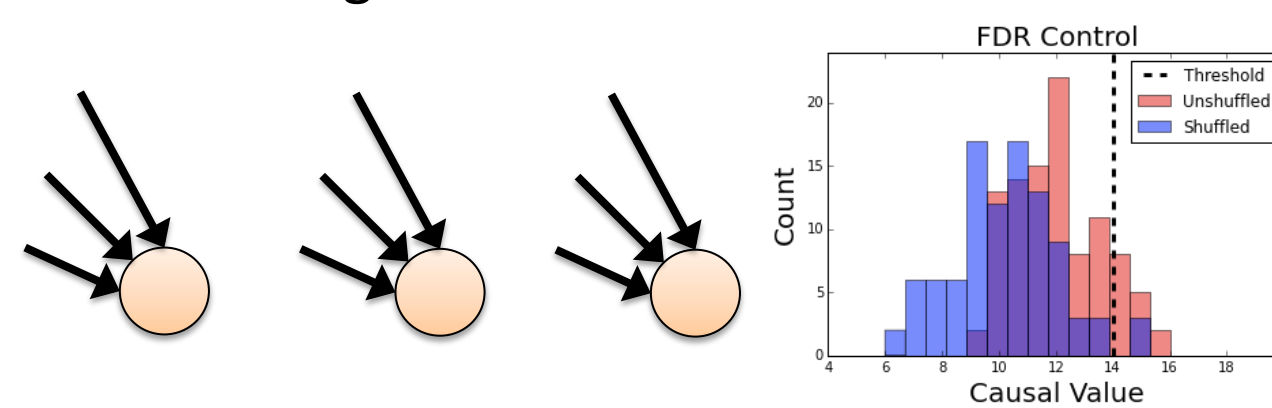
Use coefficients fit over permuted data for null



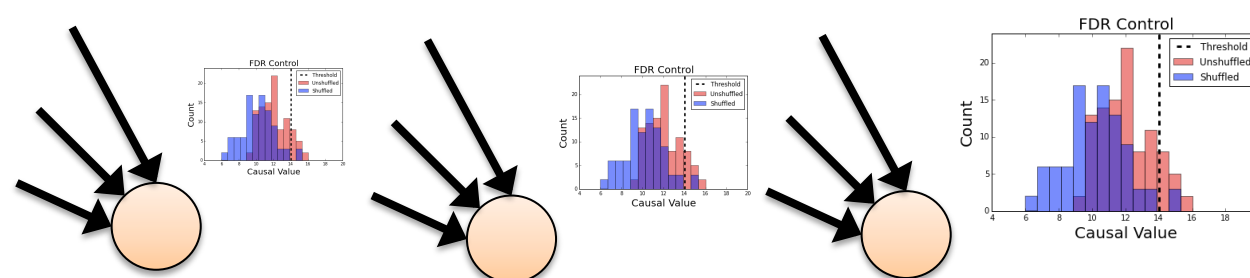
False Discovery Control

2 types of permutation FDR.

- Global FDR: global threshold over all coefficients

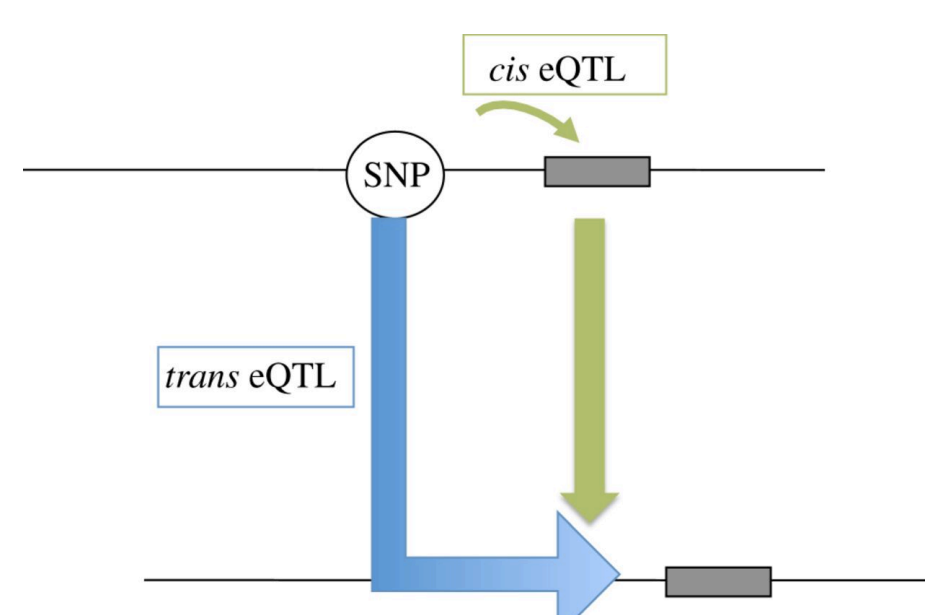


- Local FDR: threshold specific to effect gene
 – Finds networks with more consistent sizes over different settings (penalties, lag)



Validation

- $X \rightarrow Y$ means X, Y not independent
- Use Association test between Y 's expression and SNP affecting X 's expression in lung Genotype Tissue Expression Data

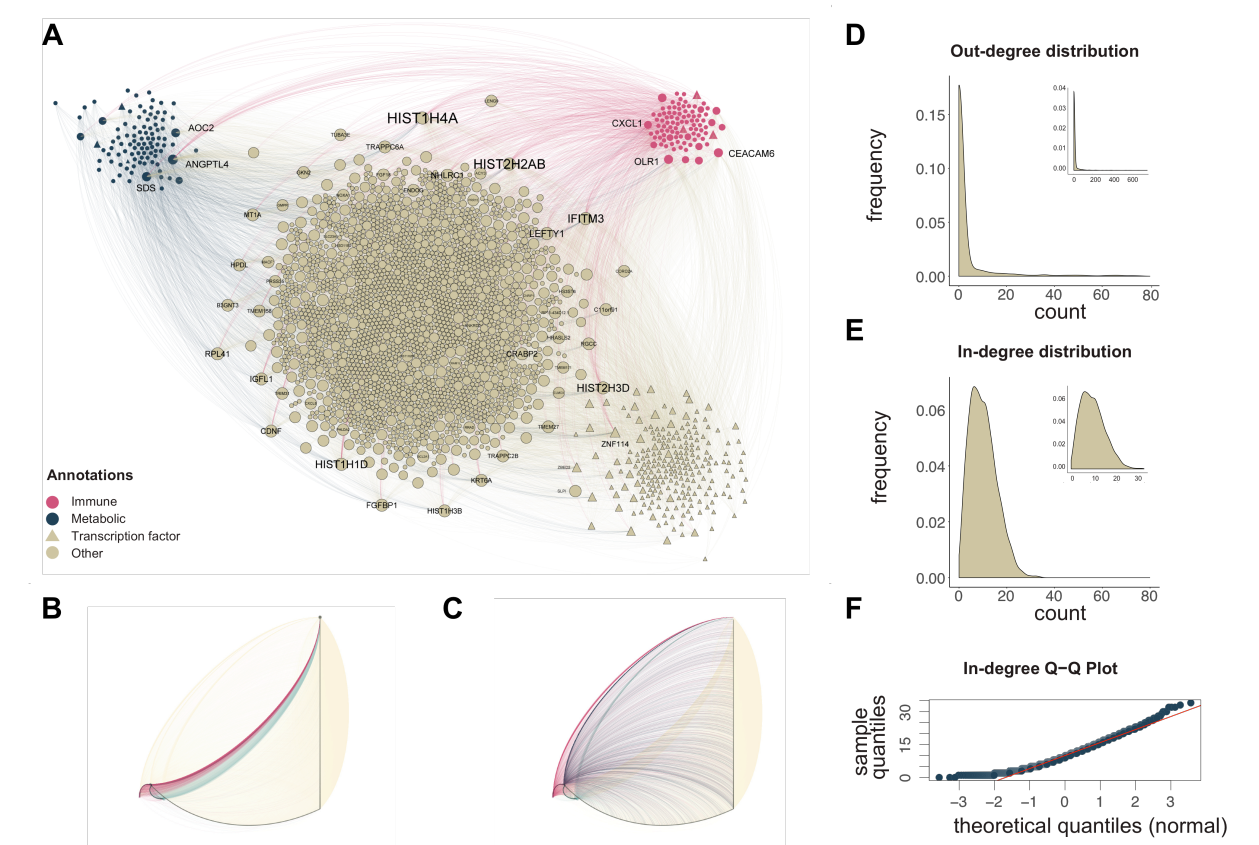


References

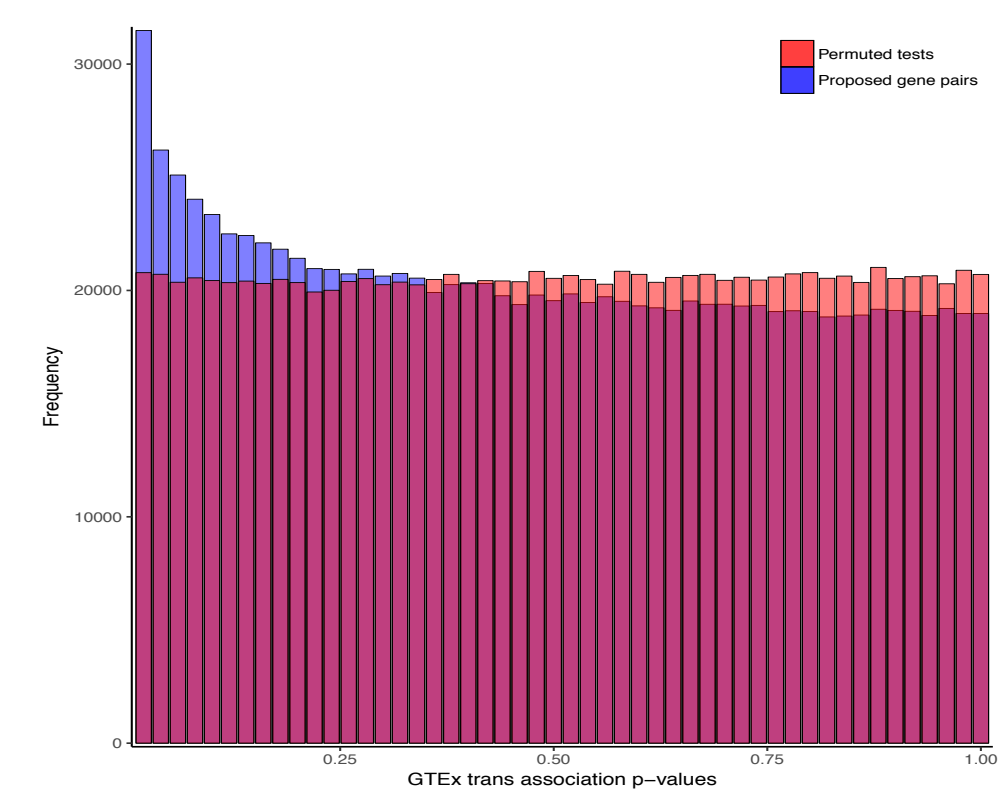
1. Nitai D. Mukhopadhyay and Snigdhanu Chatterjee. Causality and pathway search in microarray time series experiment. *Bioinformatics*, 23(4):442, 2007.
2. Gary H.F. Tam, Chunqi Chang, and Yeung Sam Hung. Application of granger causality to gene regulatory network discovery. In *IEEE 6th International Conference on Systems Biology (ISB)*, ISB '12, 2012.
3. Aurélie C Lozano, Naoki Abe, Yan Liu, and Saharon Rosset. Grouped graphical granger modeling for gene expression regulatory networks discovery. *Bioinformatics*, 25(12):1110–1118, 2009

Results

- 27,781 edge network
- 617 causal genes, 2744 effect genes
- Power-law out-degree distribution
- Normal in-degree distribution



- 280 validated edges (FDR 0.2)
- 81 edges in lung

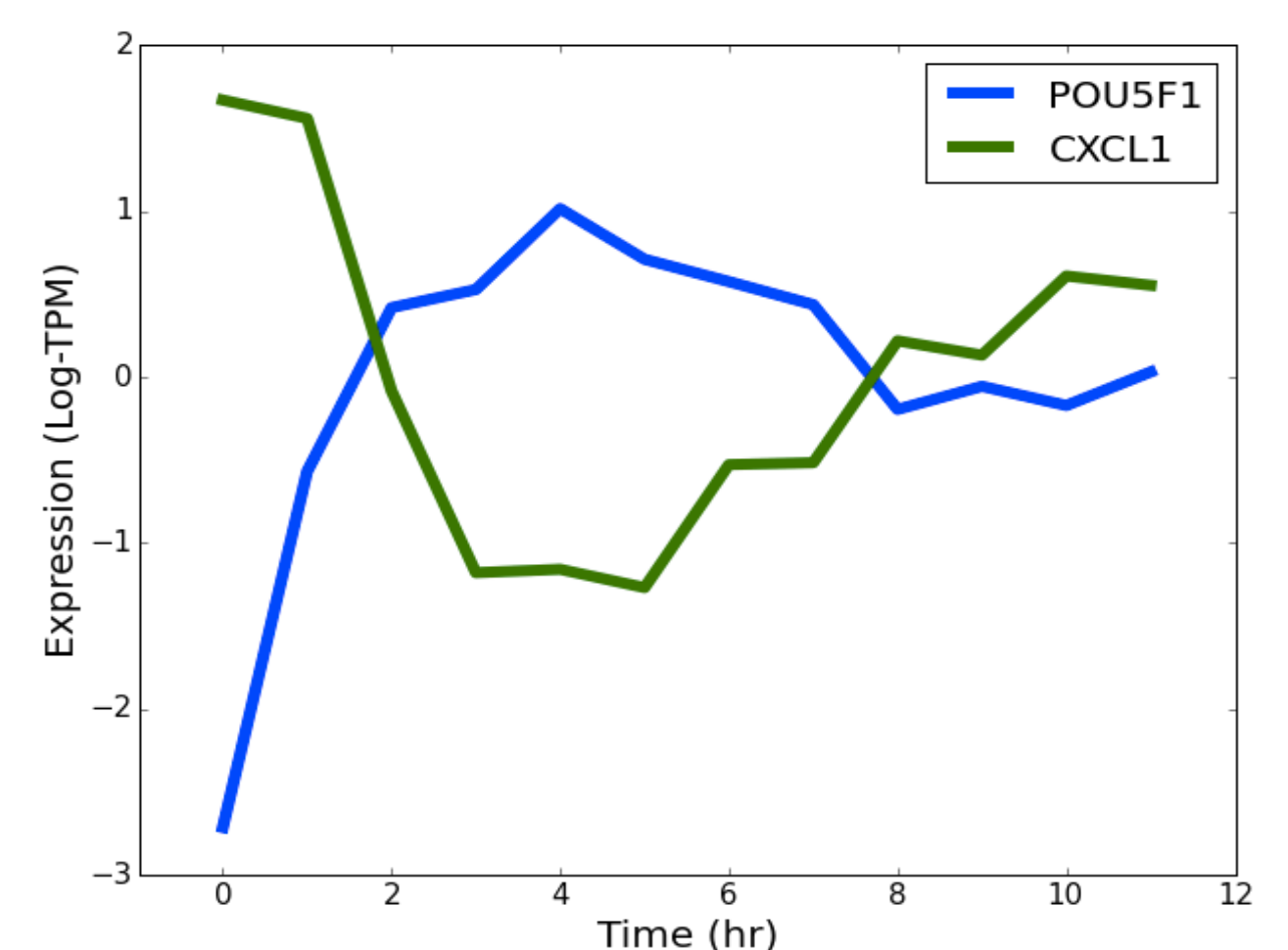


- Enrichment for Immune-Causal and Metabolic-Causal Edges

Network Edge Statistics

Edge Type	Total	%	Odds Ratio
TF-Causal	1931	7	0.8
TF-Effect	2393	8.6	1.1
Immune-Causal	2119	7.6	2
Immune-Effect	1047	3.8	1
Metabolic-Causal	2271	8.2	2
Metabolic-Effect	1211	4.4	1

- Strong repressive relation between Transcription Factor POU5F1 and Immune-related gene CXCL2



Conclusion & Future Work

- We have developed an improved pipeline for causal network inference that validates on external data.
- **Extension 1:** Use the network to suggest genes for perturbation in follow-up experiments
- **Extension 2:** Extend model to incorporate causal relations learned from data under multiple conditions

4. Ali Shojaie and George Michailidis. Discovering graphical granger causality using the truncating lasso penalty. *Bioinformatics*, 26(18):1517–1523, 09 2010.
5. Shun Yao, Shinjae Yoo, and Dantong Yu. Prior knowledge driven granger causality analysis on gene regulatory network discovery. *BMC Bioinformatics*, 16:273, 2015.
6. C.W.J. Granger. Testing for causality. *Journal of Economic Dynamics and Control*, 2:329 – 352, 1980.